

# Information Span in Credit Market Competition

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Would you give this guy a loan?



## Would you give this guy a loan?

- Suppose that  $\theta \in \{0, 1\}$  is whether or not you get repaid.
- Suppose further that  $\theta = \theta_H \times \theta_S$  where  $\theta_H$  and  $\theta_S \in \{0, 1\}$ .
- $\theta_H$  could be: Will Savitar have the money to repay the loan?
- $\theta_S$  could be: Is Savitar a good guy?
- 4 possibilities.

# Would you give this guy a loan?



# Would you give this guy a loan?

- $\theta_H$  and  $\theta_S$  unobservable.
- Can collect hard data to help figure out  $\theta_H$ :
  - How much money does Savitar have now?
  - What is his salary?
  - etc...
- Can collect soft data to help figure out  $\theta_S$ :
  - Does Savitar have friends?
  - Do his students/colleagues like him?
  - etc...
- Can get signals from hard/soft data on  $\theta_H$  and  $\theta_S$ .

## What happens if there's overlap?

- Suppose that  $\theta = \theta_H \times \theta_O \times \theta_S$  ( $\theta_O$  also Bernoulli).
- The hard data/signal you collect tells you about  $\theta_H \times \theta_O$ .
- The soft data/signal you collect tells you about  $\theta_O \times \theta_S$ .
- $\theta_O$  is a variable that impacts both hard and soft signals.
- $\theta_O$  could be: Will Savitar be alive to repay the loan?

# What happens if there's overlap?

- Medical records used to be unavailable, but now available.
- What's the difference between:

$$\theta = \theta_H \times \theta_O \times \theta_S$$

$$\theta = (\theta_H \times \theta_O) \times (\theta_S \times \theta_O)$$

- Is the  $\theta_O$  hard or soft?

# SETUP

Compare two settings:

$$\theta = \overbrace{\theta_H}^{\text{hard}} \times \underbrace{\theta_O \times \theta_S}_{\text{soft}}$$

and

$$\theta = \overbrace{\theta_H \times \theta_O}^{\text{hard}} \times \underbrace{\theta_S}_{\text{soft}}$$



## Three Agents with Different Info (first setting)

Firm:

$$\hat{\theta}_{firm} = \theta$$

Specialized Lender:

$$\hat{\theta}_{spec} = f(\hat{\theta}_H, \hat{\theta}_{soft})$$

General Lender:

$$\hat{\theta}_{gen} = f(\hat{\theta}_H, \mathbb{E}[\theta_O \times \theta_S])$$

## Three Agents with Different Info (second setting)

Firm:

$$\hat{\theta}_{firm} = \theta \text{ (unchanged)}$$

Specialized Lender:

$$\hat{\theta}_{spec} = f(\hat{\theta}_H, \hat{\theta}_{soft}) \Rightarrow f(\hat{\theta}_{hard}, \hat{\theta}_{soft})$$

General Lender:

$$\hat{\theta}_{gen} = f(\hat{\theta}_H, \mathbb{E}[\theta_O \times \theta_S]) \Rightarrow f(\hat{\theta}_{hard}, \mathbb{E}[\theta_S])$$

# Key Mechanisms

As a  $\theta_O$  moves from being 'soft' to 'hard':

## 1 More hard data

- $\Rightarrow \hat{\theta}_{gen} \rightarrow \hat{\theta}_{firm}$  less asymmetry between lender and borrower
- $\Rightarrow \hat{\theta}_{gen} \rightarrow \hat{\theta}_{spec}$  less asymmetry between lenders
- $\Rightarrow$  improved learning from competition.
- $\Rightarrow$  reduced loan rates, improved profits for general lender.

## 2 More 'span'

- $\Rightarrow \rho(\hat{\theta}_{hard}, \hat{\theta}_{soft}) > 0$
- $\Rightarrow$  Cross-learning from signals by specialized lender.

## Setup: Reminder

Compare two settings:

$$\theta = \overbrace{\theta_H}^{\text{hard}} \times \underbrace{\theta_O \times \theta_S}_{\text{soft}}$$

and

$$\theta = \overbrace{\theta_H \times \theta_O}^{\text{hard}} \times \underbrace{\theta_S}_{\text{soft}}$$

For some concreteness, suppose  $q_H = q_O = q_S = 0.8$  (span goes from 0 to 0.2).

## Philosophical Issue 1: What if most rich guys are jerks?

First setting:

$$\begin{aligned} \text{Cov}(\theta_h, \theta_s) &= \text{Cov}(\theta_H, \theta_O \times \theta_S) \\ &= 0 \end{aligned}$$

Second setting:

$$\begin{aligned} \text{Cov}(\theta_h, \theta_s) &= \text{Cov}(\theta_H \times \theta_O, \theta_O \times \theta_S) \\ &= \text{Var}(\theta_O) \\ &= 0.16 > 0 \end{aligned}$$

Hard and soft data must be positively correlated in model. Feature/bug of O-Ring setup.

## Philosophical Issue 2: How does hard data processing work?

The process of 'hardening' means new hard data is available (digitized medical records)

- *Must* get aggregated signal about  $\theta_H \times \theta_O$ .
- Independent factors, but all data bundled. (Modulo section 5.2)
- Specialization does not improve  $\alpha$  on new hard data.
- Soft data still collected as before.
- What is  $\alpha$ ?

## Philosophical Issue 2: How does hard data processing work?

What if we allowed for characteristic-specific signals?

- In first setting:
  - $h_H$  for  $\theta_H$
  - $s_O$  and  $s_S$  for  $\theta_O$  and  $\theta_S$ , respectively.
- in second setting
  - $h_H$  and  $h_O$  for  $\theta_H$  and  $\theta_O$ , respectively.
  - $s_O$  and  $s_S$  for  $\theta_O$  and  $\theta_S$ , respectively.
- Hardening  $\theta_O$  means the 'more' results hold. The 'span' results do not hold.

## Philosophical Issue 2: How does hard data processing work?

How can we preserve span results? Perhaps reasonable to get aggregated signal on soft data:

- In first setting:
  - $h_H$  for  $\theta_H$
  - $s$  for  $\theta_O \times \theta_S$ .
- in second setting
  - $h_H$  and  $h_O$  for  $\theta_H$  and  $\theta_O$ , respectively.
  - $s$  for  $\theta_O \times \theta_S$ .
- Hardening  $\theta_O$  means the 'more' and 'span' results hold. But now  $\theta_H$  is pointless.



## Philosophical Issue 3: Precise definitions

What is data? What is a signal? What is a fundamental state? What is information?

- $\theta$ s are the fundamental states.
- Directly input into 'information technology'!
- IT also takes data (not modelled) generated by fundamental and creates signal.
- Hardening described as IT progress?  $\alpha$  held fixed.
- 'hard objective data points, i.e. hard signals'.
- How can it be objective and different across lenders?

## Non-Philosophical Issue

- Before  $\theta_O$  is 'hardened',  $q_h = 0.8$ ,  $q_s = 0.64$ ,  $\eta = 0$ .
- After  $\theta_O$  is 'hardened',  $q_h = 0.64$ ,  $q_s = 0.64$ ,  $\eta = 0.2$
- Probability of fail signal before is  $0.2\alpha + (1 - \alpha)0.8$ .
- Probability of fail signal after is  $0.36\alpha + (1 - \alpha)0.64$ .
- Strictly higher! (if  $\alpha = 1$ , probability of  $LL$  goes from 4% to 12.96%).
- Countervailing force: conditional on high signal, more cross-learning about soft!

## Non-Philosophical Issue

- Hardening of data reduces credit? Possibly counterfactual.
- Also contradicts paper's Figure 5.
- In this example  $\eta$  goes from 0 to 0.2, with  $q_H$ ,  $q_O$ ,  $q_S$  fixed.
- So  $\eta \uparrow$  implies  $q_h \downarrow$ ,  $q_s = q_S \times q_O$  unchanged.
- But all figures in paper hold  $q_h$  and  $q_s$  fixed while varying  $\eta$ . So  $q_h^h \uparrow$  as  $\eta \uparrow$ ?
- To keep  $q_h$  fixed at 0.8, requires simultaneous increase of  $q_H$  from 0.8 to 1.

## Miscellaneous - Free Disposal

- O-Ring theory of credit seems difficult to justify. Not necessarily super important in terms of being pivotal for your results (apart from the correlation point earlier).
- Hard to understand purpose (mathematical or intuitional) of having differential signal structures for hard and soft information. Hard data can surely get you a continuous signal, just as a soft report can give you a go/no go recommendation. Is the soft continuity to get smooth changes in results?
- The fact that soft data collection is unaffected by span seems to imply that results will be sensitive to (soft) information acquisition costs. Some discussion of this would be helpful.
- A clear example of what a hardened fundamental  $\theta$  could be would be extremely useful to fixing ideas, and would help understand what definition you ascribe (data/signal/etc) to what real-world features.

# Summary

- Really interesting framework, with some novel mechanisms at play.
- Thinking about information span as opposed to precision or quantity is important.
- Concerns:
  - Side-effects of O-ring theory.
  - How *precisely*,  $\alpha$  is meant to be interpreted vis-a-vis data processing.
  - Confusing language around overlapping terms (fundamental, information, data, signal).
  - Confusion around figures with varying  $\eta$  while fixing  $q_h$ .